

York County School Division

# Geometry SOL Review

Student Name \_\_\_\_\_

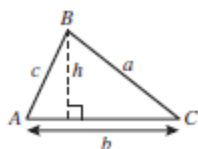
Geometry SOL Test Date – \_\_\_\_\_

Revised August, 2012

# Geometry Formula Sheet

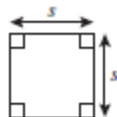
## 2009 Mathematics Standards of Learning

### Geometric Formulas



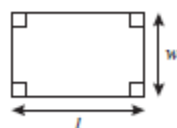
$$A = \frac{1}{2}bh$$

$$A = \frac{1}{2}ab \sin C$$



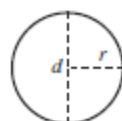
$$p = 4s$$

$$A = s^2$$



$$p = 2l + 2w$$

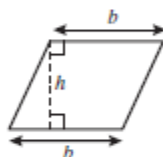
$$A = lw$$



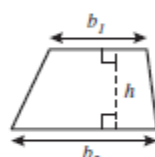
$$C = 2\pi r$$

$$C = \pi d$$

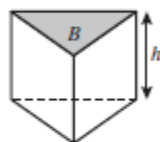
$$A = \pi r^2$$



$$A = bh$$



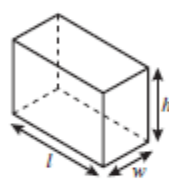
$$A = \frac{1}{2}h(b_1 + b_2)$$



$$V = Bh$$

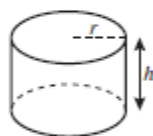
$$L.A. = hp$$

$$S.A. = hp + 2B$$



$$V = lwh$$

$$S.A. = 2lw + 2lh + 2wh$$



$$V = \pi r^2 h$$

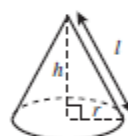
$$L.A. = 2\pi rh$$

$$S.A. = 2\pi r^2 + 2\pi rh$$



$$V = \frac{4}{3}\pi r^3$$

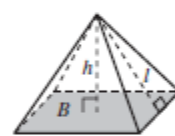
$$S.A. = 4\pi r^2$$



$$V = \frac{1}{3}\pi r^2 h$$

$$L.A. = \pi rl$$

$$S.A. = \pi r^2 + \pi rl$$



$$V = \frac{1}{3}Bh$$

$$L.A. = \frac{1}{2}lp$$

$$S.A. = \frac{1}{2}lp + B$$

### Abbreviations

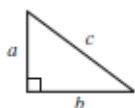
Area	A
Area of Base	B
Circumference	C
Lateral Area	L.A.
Perimeter	p
Surface Area	S.A.
Volume	V

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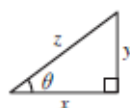
# Geometry Formula Sheet

## 2009 Mathematics Standards of Learning

### Geometric Formulas



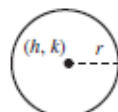
$$a^2 + b^2 = c^2$$



$$\sin \theta = \frac{y}{z}$$

$$\cos \theta = \frac{x}{z}$$

$$\tan \theta = \frac{y}{x}$$



$$(x - h)^2 + (y - k)^2 = r^2$$

**Pi**

$$\pi \approx 3.14$$

$$\pi \approx \frac{22}{7}$$

### Quadratic Formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}, \text{ where } ax^2 + bx + c = 0 \text{ and } a \neq 0$$

### Geometric Symbols

Example	Meaning
$m\angle A$	measure of angle $A$
$AB$	length of line segment $AB$
$\overrightarrow{AB}$	ray $AB$
	right angle
$\overline{AB} \parallel \overline{CD}$	Line $AB$ is parallel to line $CD$ .
$\overline{AB} \perp \overline{CD}$	Line segment $AB$ is perpendicular to line segment $CD$ .
$\angle A \cong \angle B$	Angle $A$ is congruent to angle $B$ .
$\triangle ABC \sim \triangle DEF$	Triangle $ABC$ is similar to triangle $DEF$ .
	Similarly marked segments are congruent.
	Similarly marked angles are congruent.

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# Reasoning, Lines, and Transformations

## SOL G.1

The student will construct and judge the validity of a logical argument consisting of a set of premises and a conclusion. This will include a) identifying the converse, inverse, and contrapositive of a conditional statement; b) translating a short verbal argument into symbolic form; c) using Venn diagrams to represent set relationships; and d) using deductive reasoning, including the law of syllogism.

### Hints and Notes

#### Conditional:

If  $p$ , then  $q$ .

$$p \rightarrow q$$

#### Inverse: Insert "nots"

If not  $p$ , then not  $q$ .

$$\sim p \rightarrow \sim q$$

#### Converse: Change order

If  $q$ , then  $p$ .

$$q \rightarrow p$$

#### Contrapositive: Change order and insert "nots"

$$\sim q \rightarrow \sim p$$

#### Symbols:

$\sim$  not

$\wedge$  and

$\vee$  or

$\rightarrow$  if then, implies

$\leftrightarrow$  if and only if

$\therefore$  therefore

#### Biconditional:

$p$  if and only if  $q$ .

$$p \leftrightarrow q$$

#### Law of Syllogism:

If  $a \rightarrow b$  and  $b \rightarrow c$ , then  $a \rightarrow c$ .

#### Law of Detachment:

If  $a \rightarrow b$  is true.

$a$  is true.

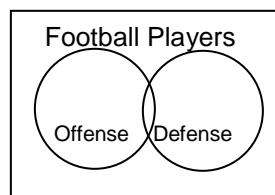
$b$  is true.

### PRACTICE G.1

1. Which is the converse of the sentence, "If Sam leaves, then I will stay."?

- A If I stay, then Sam will leave.
- B If Sam does not leave, then I will not stay
- C If Sam leaves then I will not stay.
- D If I do not stay, then Sam will not leave

2. According to the Venn Diagram, which is true?



- A Some football players play offense and defense
  - B All football players play defense
  - C No football players play offense and defense
  - D All football players play offense or defense
3. Let  $a$  represent "x is an even number."  
Let  $b$  represent "x is a multiple of 4."  
When  $x = 10$ , which of the following is true?
- A  $a \wedge b$
  - B  $a \wedge \sim b$
  - C  $\sim a \wedge b$
  - D  $\sim a \wedge \sim b$
4. Which statement is the inverse of "If the waves are small, I do not go surfing"?
- A If the waves are not small, I do not go surfing.
  - B If I do not go surfing, the waves are small.
  - C If I go surfing, the waves are not small.
  - D If the waves are not small, I go surfing.

	<p><b>5. What conclusion can be drawn from these statements</b></p> <p><b>“If negotiations fail, the baseball strike will not end.”</b>  <b>“If the baseball strike does not end, the World Series will not be played”</b></p> <p><b>A</b> If the baseball strike ends, the World Series will not be played  <b>B</b> If negotiations do not fail, the baseball strike will not end.  <b>C</b> If negotiations fail, the World Series will not be played  <b>D</b> If negotiations fail, the World Series will be played</p> <p><b>6. According to the Venn diagram, which statement is true</b></p> <div data-bbox="841 674 1182 877" data-label="Diagram"> <p>The diagram consists of a rectangle with the word 'Trapezoid' written to its upper left. Inside the rectangle, on the right side, is an oval. Below the oval, the words 'Isosceles Trapezoid' are written.</p> </div> <p><b>A</b> No trapezoids are isosceles trapezoids  <b>B</b> Some trapezoids are isosceles trapezoids  <b>C</b> All trapezoids are isosceles trapezoids  <b>D</b> Some isosceles trapezoids are parallelograms</p> <p><b>7. Which statement is logically equivalent to the true statement</b></p> <p><b>“If it is warm, then I will go swimming.”</b></p> <p><b>A</b> If I go swimming, then it is warm.  <b>B</b> If it is warm, then I do not go swimming.  <b>C</b> If I do not go swimming, then it is not warm.  <b>D</b> If it is not warm, then I do not go swimming.</p>
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**G.1 SKILLS CHECKLIST:** *I can...*

- ☐ Identify the converse, inverse and contrapositive of a conditional statement.
- ☐ Translate verbal arguments into symbolic form.
- ☐ Determine the validity of a logical argument.
- ☐ Use deductive reasoning (Law of Syllogism, Law of Detachment, Counterexamples)
- ☐ Select and use methods of reasoning and proofs.
- ☐ Interpret Venn Diagrams and represent set relationships.
- ☐ Use and recognize symbols of logic including  $\rightarrow$ ,  $\leftrightarrow$ ,  $\sim$ ,  $\therefore$ ,  $\wedge$ , and  $\vee$ .

**SOL G.2**

The student will use the relationships between angles formed by two lines cut by a transversal to a) determine whether two lines are parallel; b) verify the parallelism, using algebraic and coordinate methods as well as deductive proofs; and c) solve real-world problems involving angles formed when parallel lines are cut by a transversal.

**HINTS AND NOTES**

To prove that 2 lines are parallel, you must be able to prove:

- corresponding angles are congruent
- OR
- alternate interior angles are congruent
- OR
- alternate exterior angles are congruent
- OR
- consecutive interior angles are supplementary
- OR
- both lines are perpendicular to the same line
- OR
- both lines are parallel to the same line
- OR
- the two lines have the same slope.

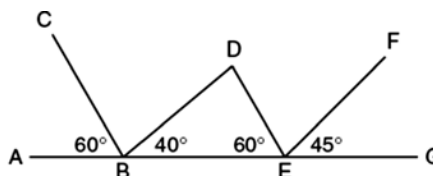
$$\text{Slope} = \frac{y_2 - y_1}{x_2 - x_1}$$

**Parallel lines** – have the same identical slope

**Perpendicular lines** – have negative reciprocal slopes

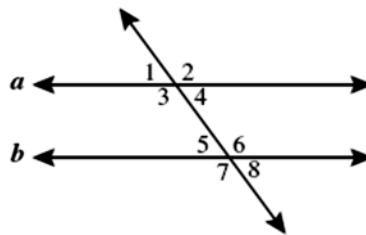
**PRACTICE G.2**

1. Using the information in the diagram, which is true?



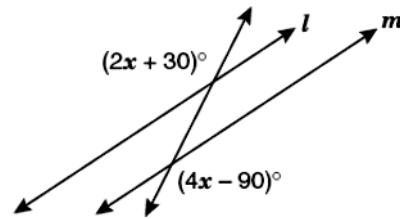
- A  $\overline{BD} \parallel \overline{EF}$
- B  $\overline{BD} \parallel \overline{DE}$
- C  $\overline{CB} \parallel \overline{BD}$
- D  $\overline{CB} \parallel \overline{DE}$

2. Line  $a$  is parallel to line  $b$  if



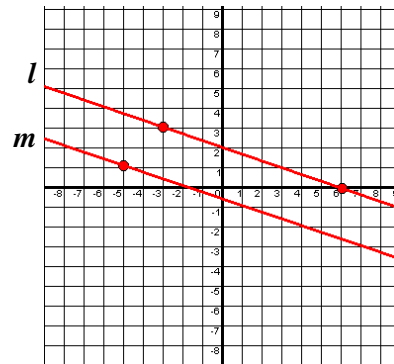
- A  $\angle 1 \cong \angle 4$
- B  $\angle 1 \cong \angle 7$
- C  $\angle 1 \cong \angle 6$
- D  $\angle 1 \cong \angle 5$

3. What value for  $x$  will show that lines  $l$  and  $m$  are parallel?



- A 60
- B 40
- C 30
- D 25

4. Prove that line  $l$  is parallel to line  $m$  using slope.



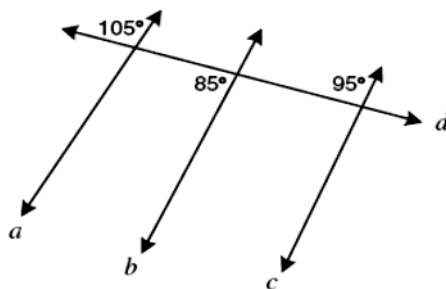
Slope of Line  $l$ :

Slope of Line  $m$ :

Why are they parallel?



5. In this diagram, line  $d$  cuts three lines to form the angles shown.



Which two lines are parallel?

- A  $a$  and  $b$
  - B  $a$  and  $c$
  - C  $b$  and  $c$
  - D No lines are parallel
6. Which statement describes the lines whose equations are  $y = \frac{1}{3}x + 12$  and  $6y = 2x + 6$ ?
- A They are segments
  - B They are perpendicular to each other
  - C They intersect
  - D They are parallel to each other

**G.2 SKILLS CHECKLIST:** *I can...*

- ☐ Verify if two lines are parallel using deductive, algebraic and coordinate proof.
- ☐ Solve problems involving intersecting lines and transversals.
- ☐ Solve real-world problems involving intersecting and parallel lines in a plane.

### SOL G.3

The student will use pictorial representations, including computer software, constructions, and coordinate methods, to solve problems involving symmetry and transformation. This will include a) investigating and using formulas for finding distance, midpoint, and slope; b) investigating symmetry and determining whether a figure is symmetric with respect to a line or a point; and c) determining whether a figure has been translated, reflected, or rotated.

#### HINTS and NOTES

**Midpoint:**  $(\frac{x_2 + x_1}{2}, \frac{y_2 + y_1}{2})$

**Slope:**  $\frac{y_2 - y_1}{x_2 - x_1}$

**Distance:**  $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

**Parallel lines have the same slope.**

**Perpendicular lines have a negative, reciprocal slope.**

#### Transformations

**Reflection** – flips over

**Translation** – slides over

**Rotation** – turns around a point

**Dilation** – shrinks or blows up

A **line of symmetry** is a line that can cut an object so that if it is folded all sides and angles will match perfectly.

#### PRACTICE G.3

1. What is the slope of the line through  $(-2, 3)$  and  $(1, 1)$ ?

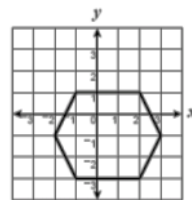
A  $-\frac{3}{2}$

B  $-\frac{2}{3}$

C  $\frac{1}{2}$

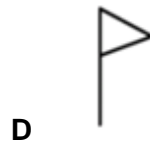
D 2

2. The hexagon in the drawing has a line of symmetry through –

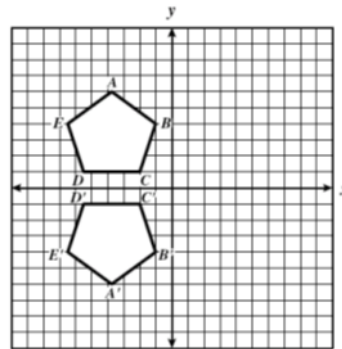


- A  $(-1, -3)$  and  $(2, 1)$   
B  $(1, 1)$  and  $(1, -3)$   
C  $(2, 3)$  and  $(2, -3)$   
D  $(-2, -1)$  and  $(3, -1)$

3. Consider the figure provided. Which of the following is a rotation in the plane of the given figure?



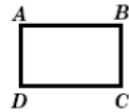
4. The polygon  $A'B'C'D'E'$  is - ?



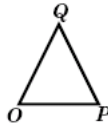
- A a translation of ABCDE across the x-axis  
 B a  $180^\circ$  clockwise rotation of ABCDE about the origin  
 C a reflection of ABCDE across the y-axis  
 D a reflection of ABCDE across the x-axis
5. Which point is the greatest distance from the origin?
- A  $(0, -2)$   
 B  $(0, -5)$   
 C  $(-2, 0)$   
 D  $(0, -12)$

6. Which polygon shown below has only one line of symmetry?

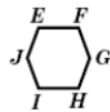
A



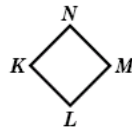
B



C



D



**G.3 SKILLS CHECKLIST:** *I can...*

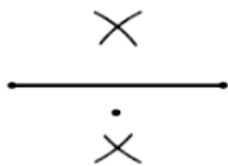
- ☐ Use midpoint formula to find the coordinates of the midpoint of a segment.
- ☐ Use a formula to find the slope of a line.
- ☐ Compare slopes to determine whether two lines are parallel, perpendicular, or neither.
- ☐ Determine if a figure has point symmetry, line symmetry, both or neither.
- ☐ Identify what type of transformation has taken place (reflection, rotation, dilation, or translation.)
- ☐ Use distance formula to find the length of a line segment given coordinates of endpoints.

## SOL G.4

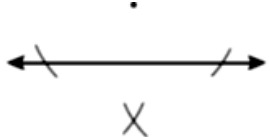
The student will construct and justify the constructions of a) a line segment congruent to a given line segment; b) the perpendicular bisector of a line segment; c) a perpendicular to a given line from a point not on the line; d) a perpendicular to a given line at a point on the line; e) the bisector of a given angle; f) an angle congruent to a given angle; and g) a line parallel to a given line through a point not on the given line.

### HINTS and NOTES

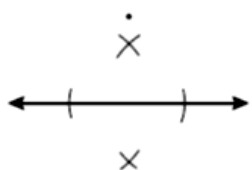
**Perpendicular bisector:**



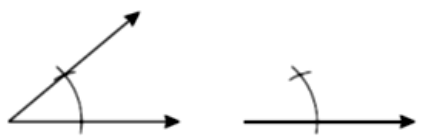
**Perpendicular bisector from a point not on the line:**



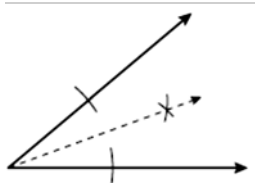
**Perpendicular to a line from a point on the line:**



**Copy an angle:**



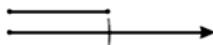
**Angle bisector:**



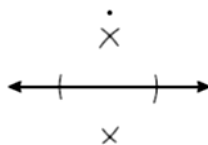
### PRACTICE G.4

1. Which drawing shows the arcs for a construction of a perpendicular segment to a line from a point not on the line?

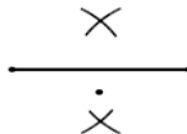
A



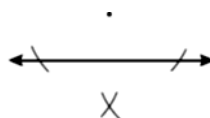
B



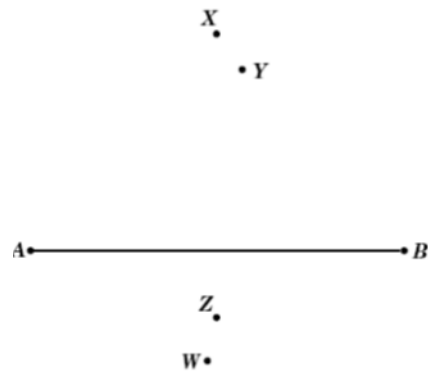
C



D

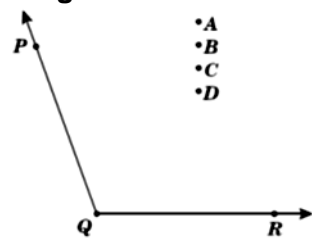


2. Which pair of points determines the perpendicular bisector of  $\overline{AB}$



- A X, W
- B X, Z
- C Y, W
- D Y, Z

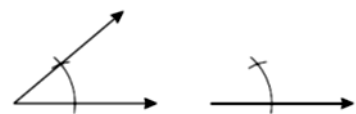
3. Use your compass and straightedge to construct a bisector of this angle.



Which point lies on the bisector?

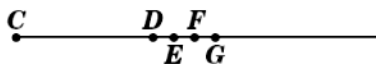
- A A
- B B
- C C
- D D

4. The drawing shows the arcs used to construct –



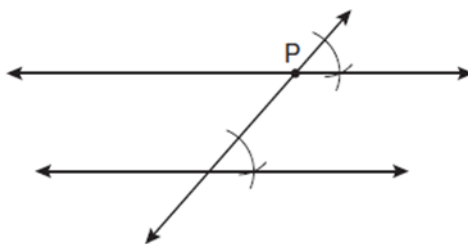
- A a bisector of a given angle
- B an angle congruent to a given angle
- C a bisector of a given line
- D a perpendicular of a line at a point on the line

5. Use your compass to answer the following question.

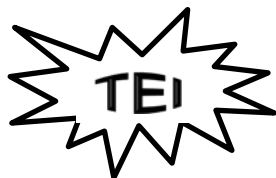


Which line segment is congruent to  $\overline{AB}$  ?

- A  $\overline{CD}$
  - B  $\overline{CE}$
  - C  $\overline{CF}$
  - D  $\overline{CG}$
6. Which geometric principle is used to justify the construction below?



- A A line perpendicular to one of two parallel lines is perpendicular to the other
- B Two lines are perpendicular if they intersect to form congruent adjacent angles
- C When two lines are intersected by a transversal and alternate interior angles are congruent, the lines are parallel
- D When two lines are intersected by a transversal and the corresponding angles are congruent, the lines are parallel



**Hot Spot Item** – You will be asked to plot points on a coordinate plane. If you don't use the “arrow” key to plot the points, your answer will not be considered answered. “AAA” (Always use the arrow key) DO NOT USE THE “DOT” KEY. Make sure you plot all points or the problem will be considered incorrect.

7. Using a compass and straightedge, construct the perpendicular of  $\overline{AB}$ . Show all construction marks.



8. Using a compass and a straightedge, construct a line that passes through point  $P$  and is perpendicular to line  $m$ . Show all construction marks.

•  $P$



**G.4 SKILLS CHECKLIST:** *I can...*

- ☐ Construct and justify the constructions of (a line segment congruent to a given line segment, the perpendicular bisector of a line segment, a perpendicular to a given line from a point not on a line, a perpendicular to a given line at a point on the line, the bisector of a given angle, an angle congruent to a given angle and a line parallel to a given line through a point not on the given line).
- ☐ Apply these constructions to possible real world applications to include:
  - Constructing equilateral triangle, square, and regular hexagon inscribed in a circle
  - Constructing inscribed and circumscribed circles of a triangle
  - Constructing a tangent line from a point outside a given circle to the circle



# Triangles

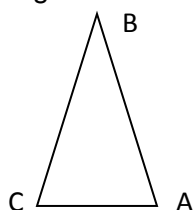
## SOL G.5

The student, given information concerning the lengths of sides and/or measures of angles in triangles, will a) order the sides by length, given the angle measures; b) order the angles by degree measure, given the side lengths; c) determine whether a triangle exists; and d) determine the range in which the length of the third side must lie. These concepts will be considered in the context of real-world situations.

### HINTS and NOTES

#### **Triangle Inequality Theorem:**

The sum of the lengths of any two sides of a triangle is greater than the length of the third side.



Ex:

$$AB + BC > AC$$

$$AC + BC > AB$$

$$AB + AC > BC$$

#### **To determine whether a triangle can exist:**

Add the 2 smallest sides and that must be greater than the third side

#### **To determine the range of a third side:**

The 3<sup>rd</sup> side must be greater than the

$$2^{\text{nd}} \text{ side} - 1^{\text{st}} \text{ side}$$

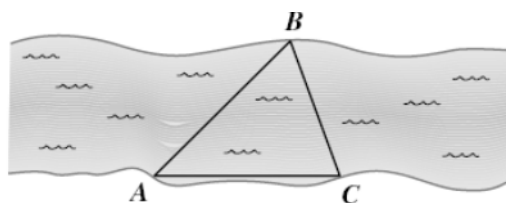
OR

less than the

$$1^{\text{st}} \text{ side} + 2^{\text{nd}} \text{ side}$$

### PRACTICE G.5

1. On the shores of a river, surveyors marked locations  $A$ ,  $B$ , and  $C$ . The measure of  $\angle ACB = 70^\circ$ , and the measure of  $\angle ABC = 65^\circ$ .



Which lists the distances between these locations in order, greatest to least?

- A**  $A$  to  $B$ ,  $B$  to  $C$ ,  $A$  to  $C$   
**B**  $B$  to  $C$ ,  $A$  to  $B$ ,  $A$  to  $C$   
**C**  $A$  to  $B$ ,  $A$  to  $C$ ,  $B$  to  $C$   
**D**  $A$  to  $C$ ,  $A$  to  $B$ ,  $B$  to  $C$
2. Which of the following could be lengths of the sides of  $\triangle ABC$  ?
- A**  $AB = 12, BC = 15, CA = 2$   
**B**  $AB = 9, BC = 15, CA = 4$   
**C**  $AB = 150, BC = 100, CA = 50$   
**D**  $AB = 10, BC = 8, CA = 12$

## HINTS & NOTES

### Comparing sides and angles of a triangle:

If one side of a triangle is longer than another side, then the angle opposite the longer side is larger than the angle opposite the shorter side and vice-versa.

#### **\*\*Remember\*\***

Biggest angle is opposite the longest side.

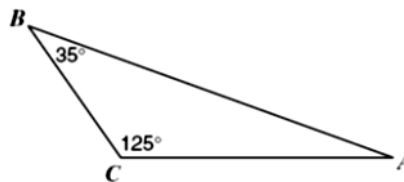
Smallest angle is opposite the shortest side.

### Make sure that you read what the question is asking for!

It might say to list in order from greatest to least or least to greatest!

**Hinge Theorem** - if two sides of one triangle are congruent to two sides of another triangle, and the included angle of the first is larger than the included angle of the second, then the third side of the first triangle is longer than the third side of the second triangle

3. In the drawing, the measure of  $\angle C = 125^\circ$  and the measure of  $\angle B = 35^\circ$ .



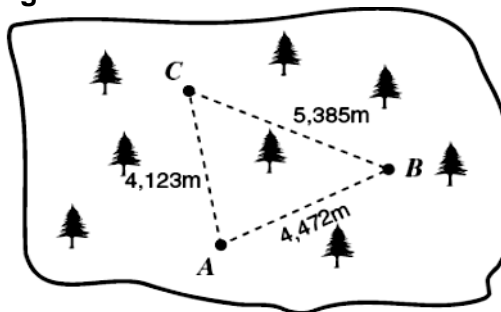
Which is the shortest side of the triangle?

- A  $\overline{AC}$
- B  $\overline{AB}$
- C  $\overline{EB}$
- D  $\overline{BC}$

4. Sara is building a triangular pen for her pet rabbit. If two of the sides measure 8 feet and 15 feet, the length of the third side could be

- A 13 ft.
- B 23 ft.
- C 7 ft.
- D 3 ft.

5. Three lookout towers are located at points A, B, and C on the section of the park in the drawing.



Which of the following statements is true concerning  $\triangle ABC$  formed by the towers?

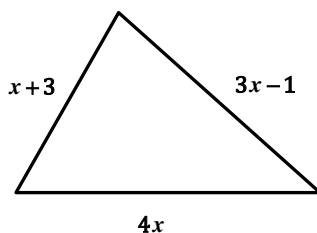
- A  $m\angle A$  is least
- B  $m\angle A$  is greatest
- C  $m\angle C$  is least
- D  $m\angle C$  is greatest

	<p>6. In any <math>\triangle XYZ</math>, which statement is always true?</p> <p>A <math>XY + YZ &lt; XZ</math></p> <p>B <math>XY + YZ &gt; XZ</math></p> <p>C <math>m\angle X + m\angle Y &lt; 90^\circ</math></p> <p>D <math>m\angle X + m\angle Y = 90^\circ</math></p>
--	---



**Put your answer in the box.** These are open-ended questions. Work them out write your answer in the box (on the computer you would type your answer in the box being sure to put it in appropriate form, simplest fraction, decimal, etc.) For our purposes, you will write your answer in the box.

7. The plot of land illustrated in the accompanying diagram has a perimeter of 34 yards. Find the length, in yards, of each side of the figure. Could these measures actually represent the measures of the sides of a triangle?



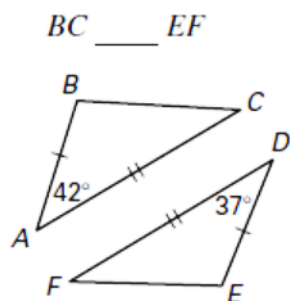

$x+3$

$4x$

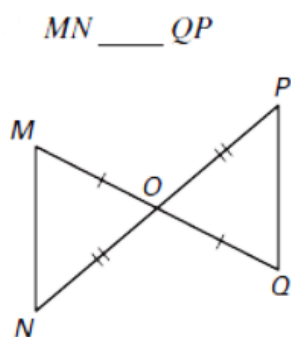
$3x-1$

Yes or No

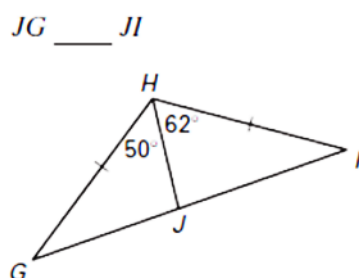
8. Complete with  $<$ ,  $>$ , or  $=$



9. Complete with  $<$ ,  $>$ ,  $=$



10.



**G.5 SKILLS CHECKLIST:** *I can...*

- ☐ Order sides of a triangle by their lengths when given the measures of the angles.
- ☐ Order the angles of a triangle by their measures when given the lengths of sides.
- ☐ Given the lengths of three segments, determine whether a triangle could be formed.
- ☐ Given the lengths of two sides of a triangle, determine the range in which the length of the third side must lie.
- ☐ Solve real-world problems given information about the lengths of sides and/or measures of angles in triangles.

**SOL G.6**

The student, given information in the form of a figure or statement, will prove two triangles are congruent, using algebraic and coordinate methods as well as deductive proofs.

**SOL G.7**

The student, given information in the form of a figure or statement, will prove two triangles are similar, using algebraic and coordinate methods as well as deductive proof.

**HINTS and NOTES**

**To prove triangles congruent:**

**SSS** (Side-Side-Side)

**SAS** (Side-Angle-Side)

**ASA** (Angle-Side-Angle)

**AAS** (Angle-Angle-Side)

**HL** (Hypotenuse-Leg)

If two triangles share a side –  
**Reflexive Property.**

**Vertical angles** are always  
congruent.

(Look for an x)

**CPCTC** – Corresponding Parts of  
Congruent Triangles are  
Congruent

**To prove triangles are similar:**

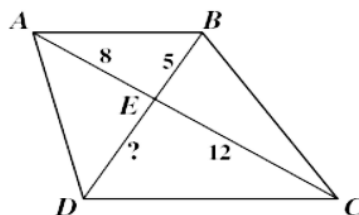
**SAS Similarity**

**SSS Similarity**

**AA Similarity**

**PRACTICE G.6 and G.7**

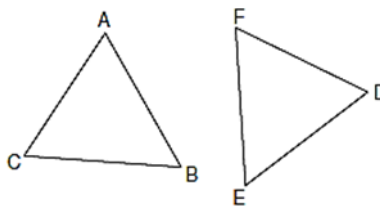
1. In the figure,  $AE = 8$ ,  $CE = 12$ , and  $BE = 5$ . What value for the measure of  $DE$  would make  $\triangle ABE$  similar to  $\triangle CDE$ ?



- A 15  
B 8  
C 7.5  
D 3.3
2. Given:  $\overline{AC} \cong \overline{BD}$  and  $\overline{AD} \cong \overline{BC}$ . Which could be used to prove  $\triangle DCA \cong \triangle CDB$ ?

- A SSS  
B SAS  
C ASA  
D AAS

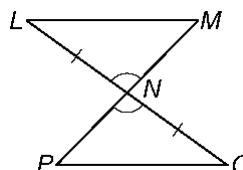
3. In the diagram of  $\triangle ABC$  and  $\triangle DEF$  below,  
 $\overline{AB} \cong \overline{DE}$ ,  $\angle A \cong \angle D$ , and  $\angle B \cong \angle E$ .



Which method can be used to prove  $\triangle ABC \cong \triangle DEF$ ?

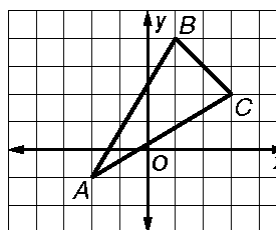
- A SSS  
B SAS  
C ASA  
D HL

4. What additional information cannot be used to prove that  $\triangle MNL \cong \triangle PNO$  ?



- A  $\overline{MN} \cong \overline{PN}$
- B  $\overline{LM} \cong \overline{OP}$
- C  $\angle M \cong \angle P$
- D  $\angle L \cong \angle O$

5. What are the vertices of a triangle congruent to the triangle in the figure?



- A  $X(4, -3), Y(-1, 0), Z(1, 2)$
- B  $D(5, 0), E(1, 3), F(-1, -2)$
- C  $G(-4, 3), H(-1, 2), I(1, 0)$
- D  $P(3, 8), Q(8, 5), R(6, 9)$

6. Which postulate or theorem shows that the triangles shown below are congruent?

A SSS

B SAS

C ASA

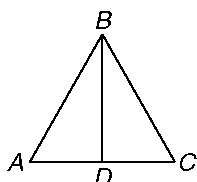
D HL



**Click and Drag.** These questions give you the choices for your answer or answers. You must click on each correct answer and drag it to the appropriate box. You must get all of them correct to get the answer correct. For our purposes, just write the correct answers in the boxes.

7. Determine the reason to justify each statement. You may choose from the Definitions, Theorems, and Postulates listed in the 2-column table.

**Given:**  $\overline{BD}$  bisects  $\angle ABC$ .  
 $\triangle ABC$  is isosceles with base  $\overline{AC}$ .  
**Prove:**  $\triangle ABD \cong \triangle CBD$

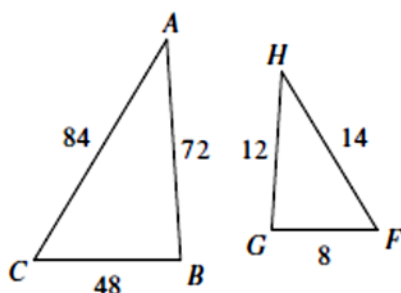


Statements	Reasons
1. $\overline{BD}$ bisects $\angle ABC$ .	1. Given
2. $\overline{BD} \cong \overline{BD}$	2.
3. $\angle ABD \cong \angle CBD$	3.
4. $\overline{AB} \cong \overline{CB}$	4.
5. $\triangle ABD \cong \triangle CBD$	5.

Given	AAS
Transitive Property of Congruence	SAS
Reflexive Property of Congruence	ASA
Symmetric Property of Congruence	SSA
If 2 sides of a triangle are congruent, then the angles opposite them are congruent	Substitution Property of Equality
Definition of Angle Bisector	Definition of Congruency
Definition of Isosceles Triangle	Reflexive Property of Equality
A Kite has 2 congruent sides	Symmetric Property of Equality



9. Determine if the pair of triangles is similar. If similar, highlight the similarity theorem to the box next to the triangle pairs. If not, then highlight “Not Similar”.

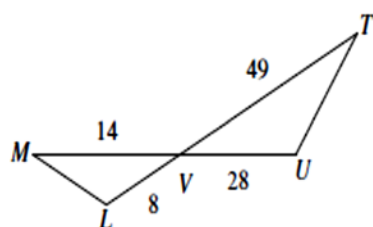


Not  
Similar

AA  
Similarity

SAS  
Similarity

SSS  
Similarity

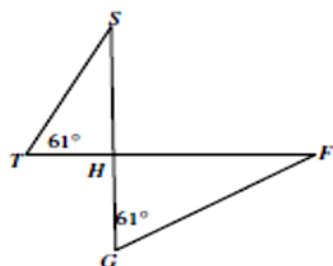


Not  
Similar

AA  
Similarity

SAS  
Similarity

SSS  
Similarity

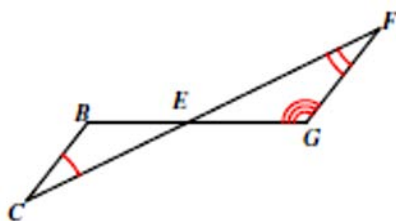


Not  
Similar

AA  
Similarity

SAS  
Similarity

SSS  
Similarity



Not  
Similar

AA  
Similarity

SAS  
Similarity

SSS  
Similarity

**G.6 and G.7 SKILLS CHECKLIST:** *I can...*

- ☐ Use definitions, postulates, and theorems to prove triangles congruent.
- ☐ Use coordinate methods, such as the distance formula and the slope formula, to prove two triangles are congruent.
- ☐ Use algebraic methods to prove two triangles are congruent.
- ☐ Use definitions, postulates, and theorems to prove triangles similar.
- ☐ Use algebraic methods to prove that triangles are similar.
- ☐ Use coordinate methods, such as the distance formula and the slope formula, to prove two triangles are similar.

**SOL G.8**

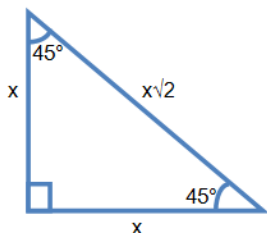
The student will solve real-world problems involving right triangles by using the Pythagorean Theorem and its converse, properties of special right triangles, and right triangle trigonometry.

**HINTS and NOTES****Pythagorean Theorem:**

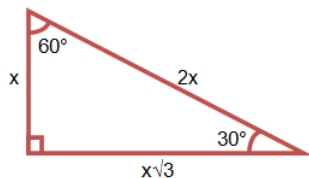
$a^2 + b^2 = c^2$ , where  $c$  is the hypotenuse and  $a$  and  $b$  are legs

**\*\*You can only use the Pythagorean theorem on RIGHT triangles.\*\***

If  $a^2 + b^2 = c^2$ , then  $\triangle ABC$  is a right triangle.

**Special Right Triangles:**  
**45°-45°-90°****Formulas:**

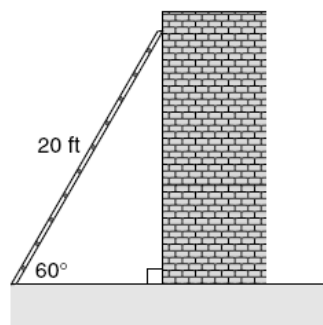
- leg = leg
- hypotenuse = leg  $\times \sqrt{2}$
- leg = hypotenuse  $\div \sqrt{2}$

**30°-60°-90°****Formulas:**

- long leg = short leg  $\times \sqrt{3}$
- hypotenuse = short leg  $\times 2$
- short leg = long leg  $\div \sqrt{3}$
- short leg = hypotenuse  $\div 2$

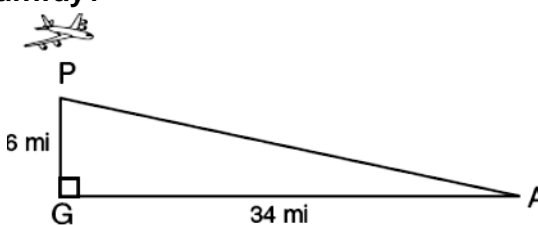
**Practice G.8**

1. A 20 foot ladder leaning against a building makes an angle of  $60^\circ$  with the ground. How far from the base of the building is the foot of the ladder?



- A 17.3 ft.  
B 10 ft.  
C 8.2 ft.  
D 5 ft.

2. An airplane is 34 ground miles from the end of a runway ( $GA$ ) and 6 miles high ( $PG$ ) when it begins approach to the airport. To the nearest mile, what is the distance ( $PA$ ) from the airplane to the end of the runway?

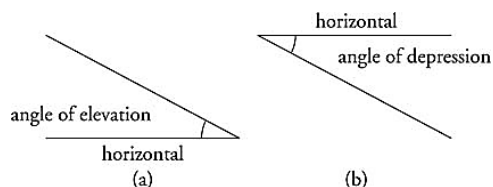


- A 35 miles  
B 37 miles  
C 39 miles  
D 41 miles

## Trigonometric Ratios:

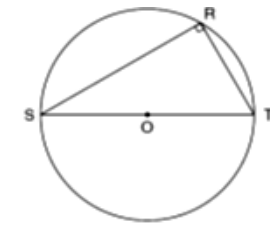
### SOH-CAH-TOA

$\sin A = \frac{\text{Opposite}}{\text{Hypotenuse}}$	Where $A$ represents the angle of reference and $A$ is never the right angle
$\cos A = \frac{\text{Adjacent}}{\text{Hypotenuse}}$	
$\tan A = \frac{\text{Opposite}}{\text{Adjacent}}$	

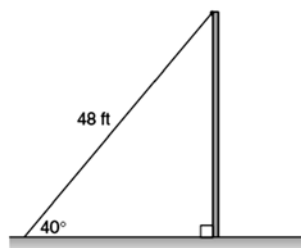


\*\*\*Use  $\sin^{-1}$ ,  $\cos^{-1}$ ,  $\tan^{-1}$  to find angles measures!

3. In circle  $O$ ,  $\angle RST$  formed by chord  $RS$  and diameter  $ST$  has a measure of  $30^\circ$ . If the diameter is 18 centimeters, what is the length of chord  $SR$ ?

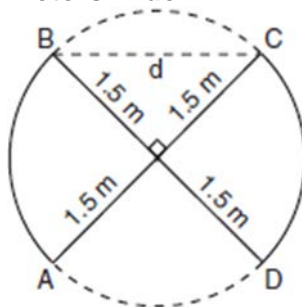


- A  $18\sqrt{3}$   
 B  $18\sqrt{2}$   
 C  $9\sqrt{3}$   
 D  $9\sqrt{2}$
4. A cable 48 feet long stretches from the top of a pole to the ground. If the cable forms a  $40^\circ$  angle with the ground. Which is closest to the height of the pole?



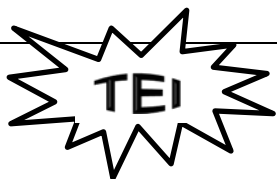
- A 40.3 ft  
 B 36.8 ft  
 C 30.9 ft  
 D 26.4 ft
5. Which set of numbers does not represent the sides of a right triangle?
- A 6, 8, 10  
 B 8, 15, 17  
 C 8, 24, 25  
 D 15, 36, 39

6. An overhead view of a revolving door is shown in the accompanying diagram. Each panel is 1.5 meters wide.



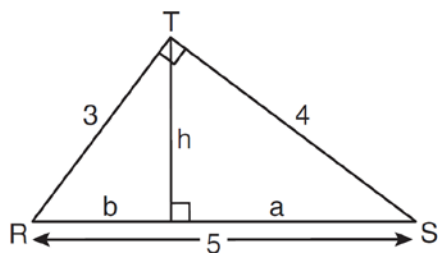
What is the approximate width of  $d$ , the opening from  $B$  to  $C$ ?

- A 1.50 meters
- B 1.73 meters
- C 3.00 meters
- D 2.12 meters



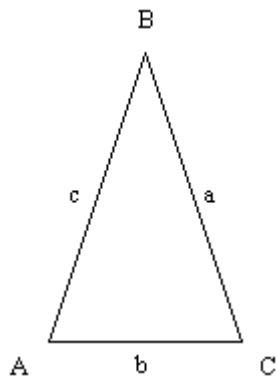
**Put your answer in the box.** These are open-ended questions. Work them out write your answer in the box (on the computer you would type your answer in the box being sure to put it in appropriate form, simplest fraction, decimal, etc.) For our purposes, you will write your answer in the box.

7. In the diagram below  $\triangle RST$  is a right triangle. The altitude,  $h$ , to the hypotenuse has been drawn. Determine the length of  $h$ .




8. Determine whether a triangle with side lengths 7, 24, and 29 is right, acute or obtuse

9. In the isosceles triangle above,  $a = 10$ ,  $c = 10$ , and  $b = 6$ . Find the measures of angles  $A$ ,  $B$ , and  $C$ .



$$m\angle A = \underline{\hspace{2cm}}$$

$$m\angle B = \underline{\hspace{2cm}}$$

$$m\angle C = \underline{\hspace{2cm}}$$

**G.8 SKILLS CHECKLIST:** *I can...*

- ☐ Determine whether a triangle formed with three given lengths is a right triangle.
- ☐ Solve for missing lengths in geometric figures, using properties of  $45^\circ - 45^\circ - 90^\circ$  triangles.
- ☐ Solve for missing lengths in geometric figures, using properties of  $30^\circ - 60^\circ - 90^\circ$  triangles.
- ☐ Solve problems involving right triangles, using sine, cosine, and tangent ratios.
- ☐ Solve real-world problems, using right triangle trigonometry and properties of right triangles.
- ☐ Explain and use the relationship between the sine and cosine of complementary angles.

# Polygons, Circles and Three- Dimensional Figures

**SOL G.9**

The student will verify characteristics of quadrilaterals and use properties of quadrilaterals to solve real-world problems.

**HINTS and NOTES**

**Quadrilateral** – polygon with four sides

**Properties:****Parallelogram:**

- Opposite sides  $\cong$
- Opposite sides parallel
- Opposite angles  $\cong$
- Consecutive angles are supplementary
- Diagonals bisect each other

**Rectangle:**

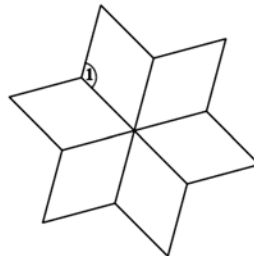
- Opposite sides  $\cong$
- Opposite sides parallel
- Opposite angles  $\cong$
- Consecutive angles are supplementary
- Diagonals bisect each other
- Four right angles ( $90^\circ$ )
- Diagonals are  $\cong$

**Rhombus:**

- Opposite sides  $\cong$
- Opposite sides parallel
- Opposite angles  $\cong$
- Consecutive angles are supplementary
- Diagonals bisect each other
- Four  $\cong$  sides
- Diagonals are perpendicular

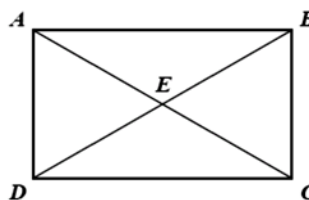
**PRACTICE G.9**

1. The design for a quilt piece is made up of 6 congruent parallelograms. What is the measure of  $\angle 1$  ?



- A  $150^\circ$
- B  $120^\circ$
- C  $60^\circ$
- D  $30^\circ$

2. Figure  $ABCD$  is a rectangle.  $\overline{AC}$  and  $\overline{BD}$  are diagonals.  $AC = 30$  meters and  $BC = 18$  meters. What is the length of  $\overline{DE}$  ?



- A 8 meters
  - B 10 meters
  - C 15 meters
  - D 24 meters
3. Which quadrilateral could have diagonals that are congruent but do not bisect each other?
- A rectangle
  - B rhombus
  - C trapezoid
  - D parallelogram

**Square:**

- Opposite sides  $\cong$
- Opposite sides parallel
- Opposite angles  $\cong$
- Consecutive angles are supplementary
- Diagonals bisect each other
- Four right angles
- Four  $\cong$  sides
- Diagonals are  $\cong$
- Diagonals are perpendicular

**Kite:**

- Diagonals are perpendicular
- One pair of opposite angles are  $\cong$

**Trapezoid:**

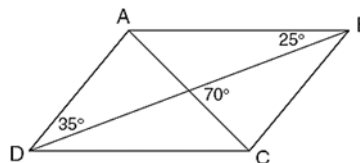
- One pair of opposite sides are parallel
- Two pairs of consecutive interior angles are supplementary

**Isosceles trapezoid:**

- One pair of opposite sides are parallel
- Two pairs of consecutive interior angles are supplementary
- One pair of opposite sides parallel
- Two pairs of consecutive angles are congruent

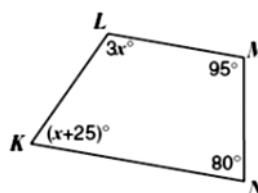
Diagonals bisect each other

4. In parallelogram  $ABCD$ , what is  $m\angle DBC$  ?



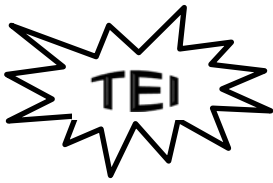
- A  $25^\circ$
- B  $35^\circ$
- C  $45^\circ$
- D  $70^\circ$

5. Given quadrilateral  $KLMN$ , what is the value of  $x$ ?



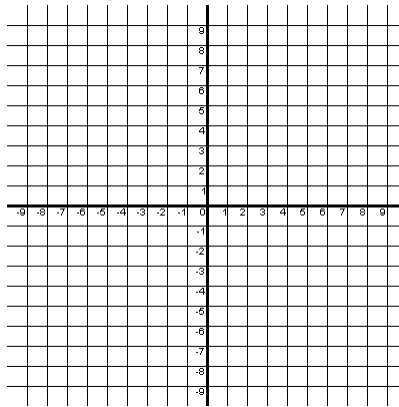
- A 35
- B 40
- C 45
- D 50





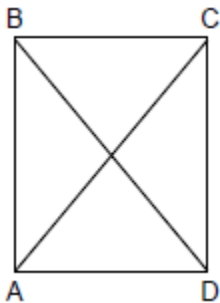
**Hot Spot Item** – You will be asked to plot points on a coordinate plane. If you don't use the “arrow” key to plot the points, your answer will not be considered answered. “AAA” (Always use the arrow key) DO NOT USE THE “DOT” KEY. Make sure you plot all points or the problem will be considered incorrect.

6. Three vertices of a parallelogram have coordinates  $(0, 1)$ ,  $(3, 7)$ , and  $(4, 4)$ . Place a point on the graph that could represent the fourth vertex of the parallelogram.

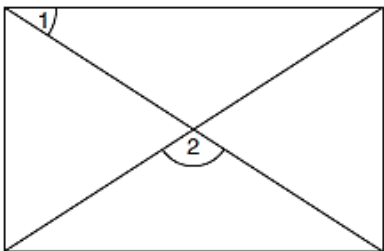


**Put your answer in the box.** These are open-ended questions. Work them out write your answer in the box (on the computer you would type your answer in the box being sure to put it in appropriate form, simplest fraction, decimal, etc.) For our purposes, you will write your answer in the box.

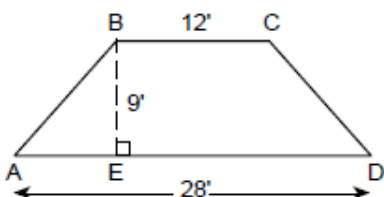
7. In the accompanying diagram of rectangle  $ABCD$ ,  $m\angle BAC = 3x + 4$  and  $m\angle ACD = x + 28$ . What is  $m\angle CAD$ ?



8. As shown in the accompanying diagram a rectangular gate has two diagonal supports. If  $m\angle 1 = 42$ , what is  $m\angle 2$ ?



9. The cross section of an attic is in the shape of an isosceles trapezoid, as shown. If the height of the attic is 9 feet,  $BC = 12$  feet, and  $AD = 28$  feet, find the length of  $AB$  to the nearest foot.



**G.9 SKILLS CHECKLIST:** *I can...*

- ☐ Solve problems, including real-world problems, using the properties specific to parallelograms, rectangles, rhombi, squares, isosceles trapezoids, and trapezoids.
- ☐ Prove that quadrilaterals have specific properties, using coordinate and algebraic methods, such as the distance formula, slope, and midpoint formula.
- ☐ Prove the characteristics of quadrilaterals, using deductive reasoning, algebraic, and coordinate methods.
- ☐ Prove properties of angles for a quadrilateral inscribed in a circle.

**SOL G.10**

The student will solve real-world problems involving angles of polygons.

**HINTS and NOTES**

Polygon	# of sides	Sum of the interior angles
Triangle	3	$180^\circ$
Quadrilateral	4	$360^\circ$
Pentagon	5	$540^\circ$
Hexagon	6	$720^\circ$
Heptagon	7	$900^\circ$
Octagon	8	$1080^\circ$
Nonagon	9	$1260^\circ$
Decagon	10	$1440^\circ$

**Sum of the exterior angles of any polygon is always  $= 360^\circ$ .**

**Remember: Number of sides = number of interior angles**

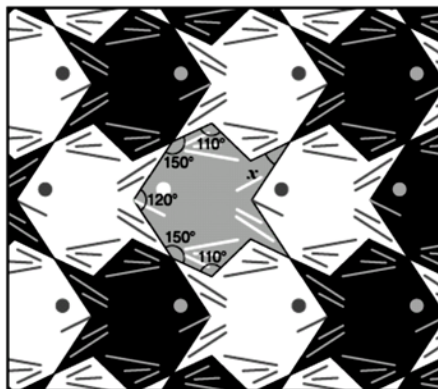
**Equilateral** – means all sides are equal

**Equiangular** - means all angles are congruent.

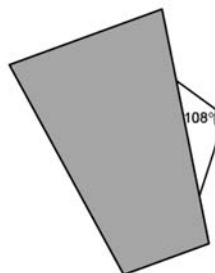
**Regular** – means all sides are equal in length and all angles are equal in measure

**Practice G.10**

1. Some of the angle measures are given for one of the fish shaped polygons in this tessellation. What is the value of  $x$ ?

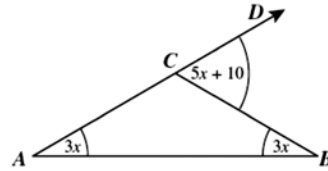


- A  $30^\circ$   
B  $40^\circ$   
C  $45^\circ$   
D  $60^\circ$
2. In the drawing, a regular polygon is partially covered by the trapezoid. How many sides does the covered polygon have?



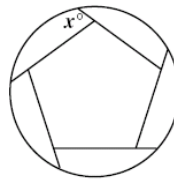
- A 8  
B 6  
C 5  
D 4

3. The figure has angle measures as shown. What is the measure of  $\angle BCD$  ?



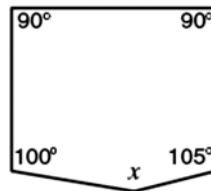
- A  $30^\circ$
- B  $60^\circ$
- C  $80^\circ$
- D  $120^\circ$

4. A floor tile is designed with a regular pentagon in the center of the tile with its sides extended. What is the value of  $x$ ?



- A  $72^\circ$
- B  $90^\circ$
- C  $110^\circ$
- D  $120^\circ$

5. What is the value of  $x$  in the pentagon?

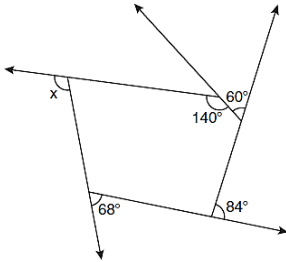


- A  $90^\circ$
- B  $155^\circ$
- C  $245^\circ$
- D  $335^\circ$

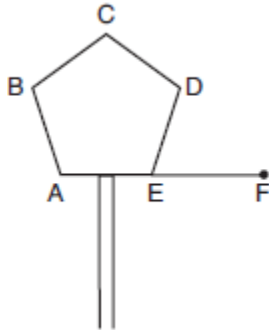


**Put your answer in the box.** These are open-ended questions. Work them out write your answer in the box (on the computer you would type your answer in the box being sure to put it in appropriate form, simplest fraction, decimal, etc.) For our purposes, you will write your answer in the box.

6. The pentagon in the diagram below is formed by five rays. What is the degree measure of  $\angle x$  ?




7. One piece of the birdhouse that Natalie is building is shaped like a regular pentagon, as shown in the accompanying diagram. If side  $AE$  is extended to point  $F$ , what is the measure of exterior angle  $DEF$ ?




8. What is the measure of an interior and exterior angle of a regular octagon?

Interior  
angle

Exterior  
angle

**G.10 SKILLS CHECKLIST:** *I can...*

- ☐ Solve real-world problems involving the measures of interior and exterior angles of polygons.
- ☐ Identify tessellations in art, construction, and nature.
- ☐ Find the sum of the measures of the interior and exterior angles of a convex polygon.
- ☐ Find the measure of each interior and exterior angle of a regular polygon.
- ☐ Find the number of sides of a regular polygon, given the measures of interior or exterior angles of the polygon.

## SOL G.11

The student will use angles, arcs, chords, tangents, and secants to a) investigate, verify, and apply properties of circles; and c) find arc lengths and areas of sectors in circles.

### HINTS and NOTES

A **circle** always measures  $360^\circ$ .

A **semi-circle** always measures  $180^\circ$ .

**Radius** – a connects the center of a circle to any point on the circle

**Radius** =  $\frac{1}{2}$  **diameter**

**Diameter** – a segment that connects any two points on a circle and passes through the center

**Diameter** = **twice the radius**

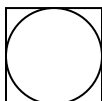
A **diameter** cuts a circle in half (makes two semi-circles)

**Chord** – a segment that connects two points on a circle

**Tangent** – a line, segment, or ray that intersects (touches) a circle in one place

**Inscribed** – means inside

Ex: a circle inscribed in a square



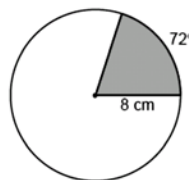
**Circumscribed** – means outside

Ex: the square is circumscribed about the circle

**Arc** – a piece of a circle

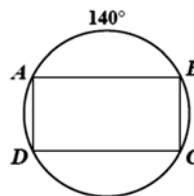
### PRACTICE G.11

1. A circle has a radius of 8 centimeters. The measure of the arc of the shaded region is  $72^\circ$ . Which is closest to the area of the shaded region of the circle?



- A  $160.8 \text{ cm}^2$
- B  $50.3 \text{ cm}^2$
- C  $40.2 \text{ cm}^2$
- D  $10.1 \text{ cm}^2$

2. Rectangle  $ABCD$  is inscribed in a circle. If the measure of the  $\widehat{AB}$  is  $140^\circ$ , what is the measure of  $\widehat{BC}$ ?



- A  $30^\circ$
- B  $40^\circ$
- C  $60^\circ$
- D  $80^\circ$

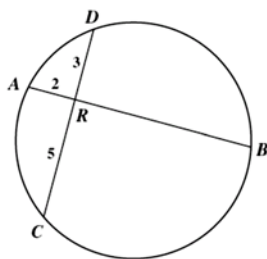
## HINTS and NOTES

### Angle Formulas:

- Tangent  $\perp$  radius
- Central angle = intercepted arc
- Inscribed angle =  $\frac{1}{2}$  intercepted arc
- Outside angle =  $\frac{1}{2}$  (big arc – little arc)
- Inside angle (makes an x) =  $\frac{1}{2}$  (intercepted arc + intercepted arc)
- Magic hat (formed by two tangents to a circle) : top of the head + tip of the hat =  $180^\circ$  and sides are congruent

**When two chords intersect in a circle** (make an x) : then part • part = part • part

Ex:

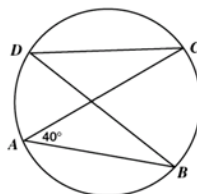


$$AR \cdot RB = CR \cdot RD$$

**When a secant intersects another secant outside of the circle:**

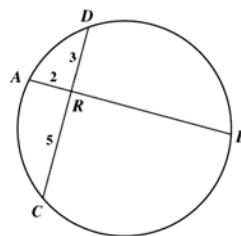
- ☐  $WO = WO$
- ☐ Whole • outside part = whole • outside part

3. If  $m\angle CAB = 40^\circ$ , what is  $m\angle CDB$  ?



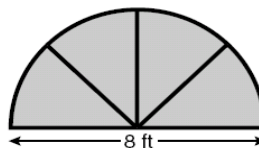
- A  $20^\circ$
- B  $40^\circ$
- C  $60^\circ$
- D  $80^\circ$

4. Chords  $\overline{AB}$  and  $\overline{CD}$  intersect at  $R$ . Using the values shown in the diagram, what is the measure of  $RB$ ?



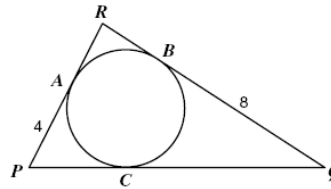
- A 6
- B 7.5
- C 8
- D 9.5

5. This is a sketch of a stained-glass window in the shape of a semicircle. Ignoring the seams, how much glass is needed for the window?

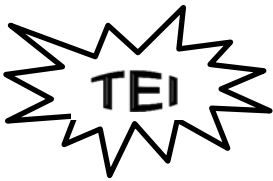


- A  $4\pi \text{ ft}^2$
- B  $8\pi \text{ ft}^2$
- C  $12\pi \text{ ft}^2$
- D  $16\pi \text{ ft}^2$

6. A, B, and C are points of tangency.  $AP = 4$  and  $BQ = 8$ . What is the measure of  $\overline{PQ}$ ?

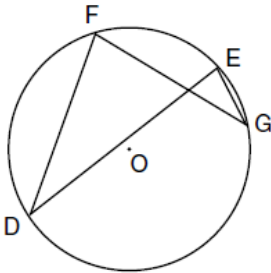


- A 4  
B 8  
C 12  
D  $\sqrt{32}$



**Highlight each correct answer.** These questions give you choices. You must click on each correct answer and make sure you mark every answer that is correct. If you forget one, it will be incorrect. Circle each correct answer. More than one answer may be selected.

7. In the diagram below of circle O, chords  $\overline{DF}$ ,  $\overline{DE}$ ,  $\overline{FG}$ , and  $\overline{EG}$  are drawn such that  $m\widehat{DF} : m\widehat{FE} : m\widehat{EG} : m\widehat{GD} = 5 : 2 : 1 : 7$ . Identify one pair of inscribed angles that are congruent to each other by highlighting the angles and give their measure.



$\angle D$	$\angle F$	$\angle E$	$\angle G$
$m\angle D = \underline{\hspace{2cm}}$	$m\angle F = \underline{\hspace{2cm}}$	$m\angle E = \underline{\hspace{2cm}}$	$m\angle G = \underline{\hspace{2cm}}$

**G.11 SKILLS CHECKLIST:** *I can...*

- ☐ Find lengths, angle measures, and arc measures associated with two intersecting chords, two intersecting secants, an intersecting secant and tangent, two intersecting tangents and central and inscribed angles.
- ☐ Calculate the area of a sector and the length of an arc of a circle, using proportions.
- ☐ Solve real-world problems associated with circles, using properties of angles, lines, and arcs.
- ☐ Verify properties of circles, using deductive reasoning, algebraic, and coordinate methods.



**SOL G.12**

The student, given the coordinates of the center of a circle and a point on the circle, will write the equation of the circle.

**HINTS and NOTES**

**Circle-** locus of points equidistant from a given point (center)

**Standard Form Equation of**

**Circle-**  $(x-h)^2 + (y-k)^2 = r^2$

Coordinates of the center of the circle are (h, k) and r is the length of the radius.

1. Write the standard equation of a circle with its center at the origin and radius of 7.

A  $x^2 + y^2 = 49$

B  $x^2 + y^2 = 14$

C  $x^2 + y^2 = 7$

D  $\frac{x^2}{14} + \frac{y^2}{14} = 1$

2. Write the standard equation of a circle with center (4, -4) and radius 4.

A  $(x-4)^2 + (y+4)^2 = 16$

B  $(x+4)^2 + (y-4)^2 = 4$

C  $(x+4)^2 - (y-4)^2 = 4$

D  $(x-4)^2 + (y-4)^2 = 16$

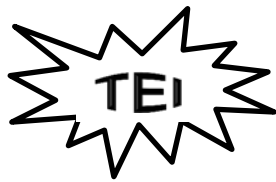
3. The standard equation of a circle with center (-4, 3) and radius 7 is \_\_\_\_.

A  $(x-4)^2 + (y+3)^2 = 7$

B  $(x+4)^2 + (y-3)^2 = 49$

C  $(x-4)^2 + (y-3)^2 = 49$

D  $(x+4)^2 + (y-3)^2 = 7$



**Put your answer in the box.** These are open-ended questions. Work them out write your answer in the box (on the computer you would type your answer in the box being sure to put it in appropriate form, simplest fraction, decimal, etc.) For our purposes, you will write your answer in the box.

4. Identify the center, radius, and diameter of a circle with the following standard equation.

$$(x - 4)^2 + (y + 10)^2 = 100$$



Center



Radius

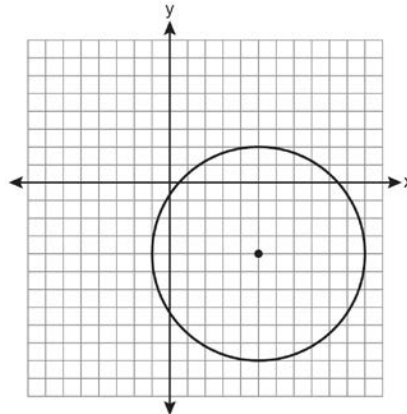


Diameter

5. Write the standard equation of a circle with center  $(-2, 5)$  and the point  $(4, 13)$  on the circle.



6. Write a standard equation of the circle graphed in the diagram graphed below.



**G.12 SKILLS CHECKLIST:** *I can...*

- ☐ Identify the center, radius, and diameter of a circle from a given standard equation.
- ☐ Use the distance formula to find the radius of a circle.
- ☐ Given the coordinates of the center and radius of the circle, identify a point on the circle.
- ☐ Given the equation of a circle in standard form, identify the coordinates of the center and find the radius of the circle.
- ☐ Given the coordinates of the endpoints of a diameter, find the equation of the circle.
- ☐ Given the coordinates of the center and a point on the circle, find the equation of the circle.
- ☐ Recognize that the equation of a circle of a given center and radius is derived using the Pythagorean Theorem.

### SOL G.13

The student will use formulas for surface area and volume of three-dimensional objects to solve real-world problems.

#### HINTS and NOTES

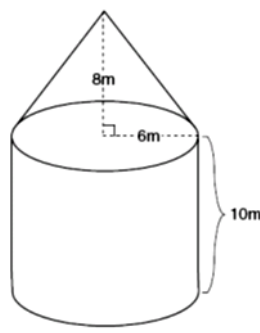
\*\*\*Use the formula sheet provided for these problems\*\*\*

**Surface area** (can also be called total area)– the amount of something that it takes to cover a figure completely  
-measured in square units

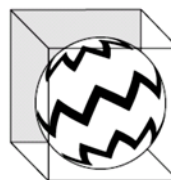
**Volume** (can also be called capacity) – the amount of space you have to fill something  
-measured in cubic units

#### PRACTICE G.13

1. Rounded to the nearest hundred cubic meters, what is the total capacity (cone and cylinder) of the storage container?

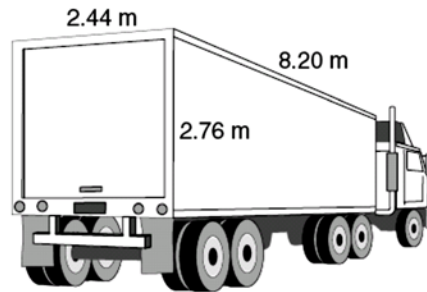


- A 1,400 cubic meters  
B 2,000 cubic meters  
C 5,700 cubic meters  
D 8,100 cubic meters
2. A sphere with a 2-inch radius is packed in a cube so that all sides touch. How much empty space is left in the cube?



- A 17.8 cu. in.  
B 30.5 cu. in.  
C 33.5 cu. in.  
D 47 cu. in.

3. The cargo space of the truck is 2.44 meters wide, 2.76 meters high and 8.20 meters long. How many cubic meters of cargo space does the truck have?



- A 26.80 cubic meters  
B 55.22 cubic meters  
C 98.75 cubic meters  
D 110.44 cubic meters
4. A spherical paintball measures 1.5 centimeters in diameter. Approximately how much paint is in it?
- A  $14.13 \text{ cm}^3$   
B  $9.42 \text{ cm}^3$   
C  $7.07 \text{ cm}^3$   
D  $1.77 \text{ cm}^3$
5. To the nearest gallon, what is the volume of a cylindrical water heater 1.4 feet in diameter and 4 feet tall? (1 cubic foot = 7.48 gallons)
- A 34 gal.  
B 46 gal.  
C 59 gal.  
D 132 gal.

**G.13 SKILLS CHECKLIST:** *I can...*

- ☐ Find the total surface area of cylinders, prisms, pyramids, cones, and spheres, using the appropriate formulas.
- ☐ Calculate the volume of cylinders, prisms, pyramids, cones, and spheres, using the appropriate formulas.
- ☐ Solve problems, including real-world problems, involving total surface area and volume of cylinders, prisms, pyramids, cones, and spheres as well as combinations of three-dimensional figures.

**SOL G.14**

The student will use similar geometric objects in two-or three dimensions to a) compare ratios between side lengths, perimeters, areas, and volumes; b) determine how changes in one or more dimensions of an object affect area and /or volume of the object; c) determine how changes in area and /or volume of an object affect one or more dimensions of the object; and d) solve real-world problems about similar geometric objects.

**HINTS and NOTES****Dimensional changes:**

height length width radius diameter perimeter circum- ference	area	volume
$a$	$a^2$	$a^3$

When finding a missing side of similar figures always set up a proportion keeping corresponding parts in the same order. Cross multiply to solve.

**Scale factor:**

Ratio of the sides  $\rightarrow \frac{a}{b}$

**Ratio of the perimeters = scale**

factor  $\rightarrow \frac{a}{b}$

**Ratio of the areas =**

(scale factor)<sup>2</sup>  $\rightarrow \frac{a^2}{b^2}$

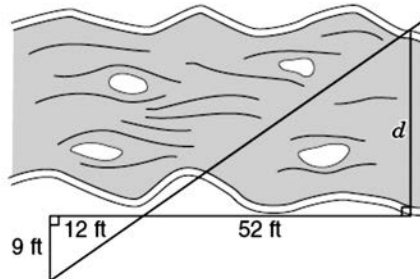
**Ratio of the volumes =**

**PRACTICE G.14**

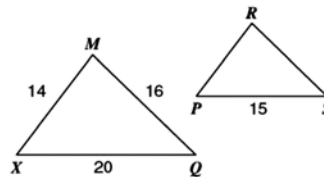
1. A cylindrical paint can has the capacity of one gallon. For another size can, the height is doubled. What is the capacity of the larger size?  
  
A 2 gal.  
B 4 gal.  
C 8 gal.  
D 16 gal.
2. If the edge of a cube is  $2x$ , the volume of the cube is:  
  
A  $8x^3$   
B  $4x^3$   
C  $2x^3$   
D  $4x^2$
3. If the radius of a circle is tripled, then the area of the circle is multiplied by:  
  
A 27  
B 9  
C 3  
D 6
4. Two similar cones have heights 5 and 20. What is the ratio of their volumes?  
  
A 1:16  
B 1:64  
C 1:4  
D 4:16

$$(\text{scale factor})^3 \rightarrow \frac{a^3}{b^3}$$

5. The distance across a river was estimated by making the measurements shown. Which is a good estimate of the distance  $d$ ?



- A 9 ft.  
B 36 ft.  
C 39 ft.  
D 69 ft.
6. The ratio of the circumference of two circles is  $\frac{3}{2}$ . The radius of the smaller circle is 8 inches. What is the radius of the larger circle?
- A  $5\frac{1}{3}$  inches  
B 6 inches  
C 9 inches  
D 12 inches
7. Which proportion can be used to find the value of  $\overline{PR}$  if  $\triangle XMQ$  is similar to  $\triangle PRS$ ?



- A  $\frac{20}{15} = \frac{14}{PR}$   
B  $\frac{10}{5} = \frac{7}{PR}$   
C  $\frac{14}{20} = \frac{15}{PR}$   
D  $\frac{15}{20} = \frac{14}{PR}$

	<p><b>8. The ratio between the volumes of two spheres is 27 to 8. What is the ratio between their respective radii?</b></p> <p><b>A</b> 81:64                                      <b>B</b> 27:16  <b>C</b> 9:8    <b>D</b> 3:2</p> <p><b>9. Two triangles are similar. The lengths of the sides of the smaller triangle are 3, 5, and 6, and the length of the longest side of the larger triangle is 18. What is the perimeter of the larger triangle?</b></p> <p><b>A</b> 14    <b>B</b> 18  <b>C</b> 24    <b>D</b> 42</p> <p><b>10. A triangle has sides whose lengths are 5, 12, and 13. A similar triangle could have sides with lengths of</b></p> <p><b>A</b> 6, 8, and 10                                      <b>B</b> 3, 4, and 5  <b>C</b> 7, 24, and 25                                      <b>D</b> 10, 24, and 26</p> <p><b>11. The ratio of the corresponding sides of similar squares is 1 to 3. What is the ratio of the area of the smaller square to the area of the larger square?</b></p> <p><b>A</b> <math>1:\sqrt{3}</math>    <b>B</b> 1:6  <b>C</b> 1:3    <b>D</b> 1:9</p> <p><b>12. Describes what happens to the volume of a cone if its radius is doubled while the height is halved. The volume is ____.</b></p> <p><b>A</b> unchanged  <b>B</b> doubled  <b>C</b> increased by a factor of <math>\frac{1}{3}</math>  <b>D</b> not able to be determined</p>
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**G.14 SKILLS CHECKLIST:** *I can...*

- ☐ Compare ratios between side lengths, perimeters, areas, and volumes, given two similar figures.
- ☐ Describe how changes in one or more dimensions affect other derived measures (perimeter, area, total surface area, and volume) of an object.
- ☐ Describe how changes in one or more measures (perimeter, area, total surface area, and volume) affect other measures of an object.
- ☐ Solve real world problems involving measured attributes of similar objects